## MA 125 CT, CALCULUS I

Test 1, February 2, 2015
Name (Print last name first):

Show all your work and justify your answer!
No partial credit will be given for the answer only!
PART I
You must simplify your answer when possible.
All problems in Part I are 7 points each.

1. Use the definition of the derivative to show that if $f(x)=x^{2}$, then $f^{\prime}(x)=2 x$.
2. Evaluate $\lim _{x \rightarrow 3} \frac{\sin (x)}{x+1}$
3. Evaluate $\lim _{x \rightarrow \infty} \frac{x^{5}+3 x^{2}-7}{-2 x^{5}+4 x^{3}-x^{2}-6}$
4. Given that $y=f(x)=x^{2}\left(x^{3}+\sqrt{x}\right)$, find $f^{\prime}(x)$.
5. Given that $y=f(x)=x^{3} \cos (x)$, find $f^{\prime}(x)$.
6. Given that $y=f(x)=\frac{x^{2}+1}{x^{2}-1}$, find $f^{\prime}(x)$.
7. Find the equation of the tangent line to the graph of $y=f(x)=\sqrt{x}$ at the point $x=4$.
8. Evaluate $\lim _{x \rightarrow 2} \frac{x^{2}-4}{x^{2}+x-6}$
9. If the position of a particle, at time $t$, is given by $S(t)=4 t^{3}+2 t$, find the acceleration at time $t=-1$. Is at that time the velocity $v(t)$ increasing or decreasing? Justify your answer.
10. Given the graph of the function below, state (a) where it is continuous and (b) where the derivative exist.


## PART II

All problems in Part II are 10 points each.

1. Evaluate
(a) $\lim _{x \rightarrow 0} \frac{\sin (5 x)}{x}$
(b) $\lim _{x \rightarrow 0} \frac{1-\cos ^{2}(x)}{x}$
2. Evaluate $\lim _{x \rightarrow \infty}\left(\sqrt{9 x^{2}+x}-3 x\right)$
3. Below you are given the graph of the derivative $f^{\prime}(x)$ of a function $y=f(x)$.
(a) State the $x$-coordinates of all points where the graph of $y=f(x)$ has a horizontal tangent line.
(b) State all $x$-values of points where the rate of change of the function $y=f(x)$ is maximal.

Graph of the derivative $f^{\prime}(x)$


